CRAIG, KELLER, AND HAMMEL



FIG. 2. Ratio of observed asymptotic  $(T_1 = T_{\lambda})$  power input to that calculated on the basis of several theories as a function of  $T_0$ ;  $d = 3.36 \mu$ . Curve a-m = 3,  $\mathbf{v}_e = 0$ , A as given by Vinen (4); curve b-m = 3,  $\mathbf{v}_e$  as given by Dash (16), A as given by Vinen; curve e-m = 3,  $\mathbf{v}_e = 0$ , A = 50 cm-sec/gm; curve d-m = 4,  $\mathbf{v}_e = 0$ , A = 50 cm-sec/gm.

to determine a few selected values of A in the region  $1.7^{\circ}-2.0^{\circ}$ K for large  $\bar{q}$  where neither of these objections applies. We have not been able to solve the nonlinear integral equation (26) directly for  $\bar{q}$ , but instead we have used a variance method pointed out to use by Dr. R. B. Lazarus.

We consider

$$\bar{\mathbf{q}}(\lambda, T) = \frac{d^2}{L} \int_{T_0}^T \frac{\Lambda}{1+\lambda\delta} d\tau$$
(44)

where  $\delta \equiv \alpha d^2 \bar{\mathbf{q}}^2$ ,  $\lambda \equiv \alpha'/\alpha$  is a factor relating  $\alpha$  (determined from Vinen's A(T)) and  $\alpha'$  (the new value of  $\alpha$  to be determined from the present experiments);  $\tau$  is a dummy variable. Holding  $\bar{\mathbf{q}}$  fixed and varying  $\lambda$  we obtain

$$0 = \frac{d^2}{L} \left[ \frac{\Lambda}{1+\lambda\delta} \left( \frac{\partial T}{\partial \lambda} \right)_{\tilde{q}} - \int_{T_0}^T \frac{\Lambda\delta}{(1+\lambda\delta)^2} d\tau \right];$$
(45)

and holding  $\lambda$  fixed and varying  $\bar{\mathbf{q}}$ 

$$\left(\frac{\partial \tilde{\mathbf{q}}}{\partial T}\right)_{\lambda} = \frac{d^2}{L} \left[\frac{\Lambda}{1+\lambda\delta} - \int_{T_0}^T \frac{2\lambda\Lambda\delta}{\tilde{\mathbf{q}}(1+\lambda\delta)^2} d\tau \left(\frac{\partial \tilde{\mathbf{q}}}{\partial T}\right)_{\lambda}\right].$$
(46)

Combining (45) and (46) we find

$$\left(\frac{\partial T}{\partial \lambda}\right)_{\bar{\mathbf{q}}} = \frac{\bar{\mathbf{q}}}{2\lambda} \left[ \left(\frac{\partial T}{\partial \bar{\mathbf{q}}}\right)_{\lambda} - \frac{(1+\lambda\delta)L}{\Lambda d^2} \right]$$
(47)

86